

AB INITIO INVESTIGATIONS AND BEHAVIOUR OF THE α -Ce₂ON₂ PHASE IN THE EXTREME PRESSURE CONDITIONS

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Abstract: Recently predicted α -phase in the Ce₂ON₂ compound has been further investigated using *ab initio* methods. The structural properties of the α -Ce₂ON₂ have been investigated and compared with the related AlCo₂Pr₂ structure. Mechanical properties including elastic constants, bulk, shear and elastic moduli, Poisson's ratio, Pugh's criterion, and hardness are calculated in the pressure range from 0 to 10 GPa. Also, electronic properties are calculated at the same pressure conditions using DFT-LDA approximation and the characteristic band structure has been analyzed.

Keywords: α -Ce₂ON₂, *ab initio*, mechanical properties, electronic properties, high pressure

1. Introduction

When investigating the materials under extreme conditions it is important to know the energy landscape concepts for chemical systems under extreme conditions, as well as materials properties investigation under extreme conditions.[1-3] Nitrogen doping is often used for oxide photocatalysts if band-gap tuning is needed.[4] In this way obtained stoichiometric oxynitrides can have useful optical properties.[5] Furthermore, the incorporation of nitrogen has been reported as an alternative method for cation doping that increases the anion vacancy concentration and stabilizes the cubic or tetragonal form of ZrO₂ at room temperature.[6] The nitrogen-doped oxides exhibit good mechanical, catalytical, and optical properties and have been reported as superionic conductors.[6]

On another side, pure ceria (CeO₂) has important technological applications, e.g., as catalysts, in electrolyte solid oxide fuel cells, oxygen storage components, mechanical polishing for microelectronics, metallurgy, and biomedicine.[7-11]. Doping of ceria with nonmetals is extremely rare, but it has been reported before, where that doping significantly changes the physical and chemical properties of ceria [12-14]. Besides doping with nitrogen, ceria has been doped with carbon, phosphorus, sulfur, magnesium, lanthanum, europium, and praseodymium.[15-18] Similarly, cerium nitride (CeN) is a material with interesting optical, electronic, and magnetic properties, related to the structure and oxidation state.[19-21]

In our previous study, we have identified stable and metastable modifications of the Ce₂ON₂ compound for the first time, using a combination of global optimization and data mining. [22] The α -Ce₂ON₂ modification, with the post-AlCo₂Pr₂ structure, is predicted to be the thermodynamically stable modification at standard conditions. In this work, we go one step forward giving the predicted structural, mechanical, and electronic properties in the high-pressure range for the not-yet-synthesized α -Ce₂ON₂ phase.

2. Computational details

Ab initio calculations of the mechanical and electronic properties in the high-pressure regime were performed using the CRYSTAL17 code [23], which is based on linear combinations of atomic orbitals. Local optimizations are performed on the density functional theory level using the local

density approximation (LDA). In the case of Ce^{4+} a pseudopotential [24] was used, together with a $[4s4p2d3f]$ basis set, for O^{2-} a $[4s3p]$ basis set was used [25, 26], and for N^{3-} $[3s2p]$ an all-electron basis set based on Gaussian-type orbitals was employed [27, 28]. A computational strategy implemented in the CRYSTAL solid-state quantum-chemical program has been performed for the accurate *ab initio* simulation of elastic properties of crystalline materials under pressure.[29] Full elastic tensor has been generated by using the keyword ELASTCON. [30, 31] Crystallographic analysis was performed using KPLOTT code,[32] and structure visualization using VESTA software [33].

3. Results and Discussion

Figure 1a shows the parent structure obtained from data mining based searches in the ICSD database [34] in the AlCo_2Pr_2 type of structure [35]. It crystallizes in the monoclinic space group $C2/c$ (no. 15) with 8-fold coordination of cobalt by Al and Pr atoms (Table 1). The structure evolved after *ab initio* structure optimization into $\alpha\text{-Ce}_2\text{ON}_2$ phase, with so-called post- AlCo_2Pr_2 type of structure, shown in Figure 1b. The new α -phase shows trigonal symmetry with the $P-3m1$ space group (no. 164) and details considering unit cell parameters and atomic positions are published elsewhere. [22]

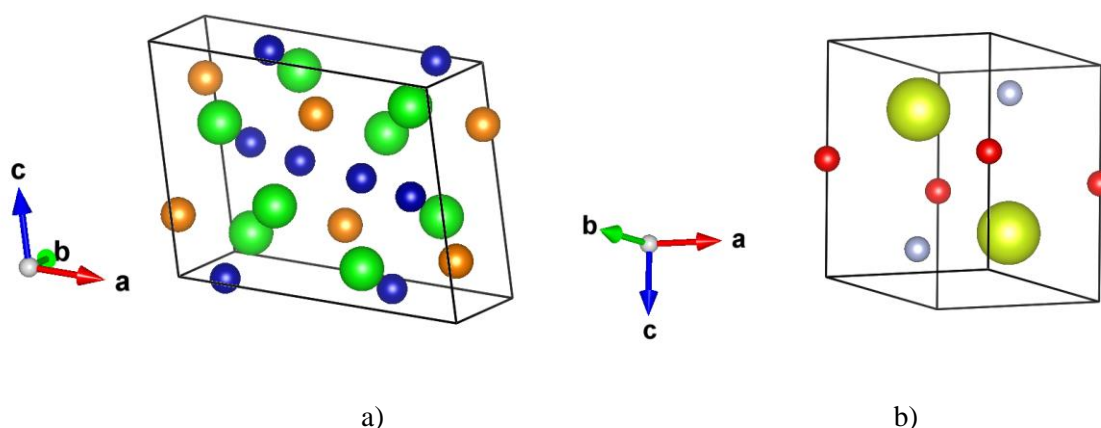


Figure 1. Crystal structure of a) AlCo_2Pr_2 type, where aluminum atoms are orange color, cobalt atoms are blue, and praseodymium atoms are green, b) $\alpha\text{-Ce}_2\text{ON}_2$ phase, where cerium is yellow, oxygen is red, and nitrogen is shown as grey balls.

Table 1. Atom distances and coordination of cobalt in the AlCo_2Pr_2 structure, and cerium in the $\alpha\text{-Ce}_2\text{ON}_2$ structure.

Co-coordination/Atom	AlCo_2Pr_2 (Å)	Ce-coordination/atom	$\alpha\text{-Ce}_2\text{ON}_2$ (Å)
Al	2.5714	N	2.2536
Al	2.5879	N	2.2536
Pr	2.9613	N	2.2536
Pr	2.9778	N	2.2752
Pr	2.9778	O	2.5674
Pr	3.0270	O	2.5674
Pr	3.0521	O	2.5674
Pr	3.0618	N	3.2944

Interestingly is that the cerium atoms are in 7-fold coordination with four nitrogen and three oxygen atoms in the $\alpha\text{-Ce}_2\text{ON}_2$ phase with the polyhedra edge-connected (Figure 2a). However, when including the second coordination polyhedra of cerium atom (distances up to 4 Å), one can observe

distant nitrogen atom at 3.2944 Å (Table 1). When plotting an additional N atom, the Ce atom becomes 8-fold coordinated in the α -phase with a square prism connected by planes (Figure 2b).

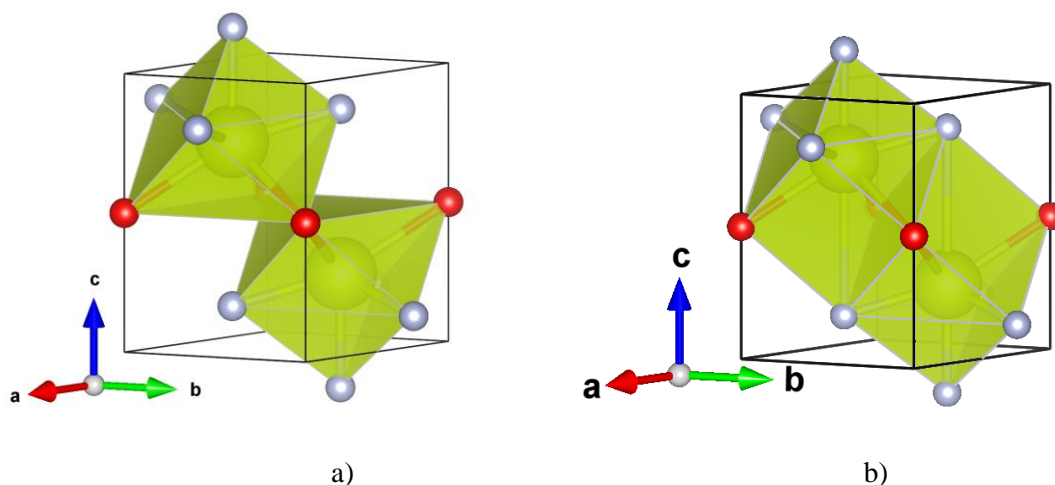


Figure 2. Crystal structure of α -Ce₂ON₂ phase with a) 7-fold coordination; b) 8-fold coordination of cerium atoms by O- and N-atoms. Note that cerium is yellow, oxygen is red, and nitrogen is shown as grey balls.

Since the α -Ce₂ON₂ structure is only theoretically predicted phase in the Ce₂ON₂ system, future experimental work is expected. In this respect, we show theoretical X-ray diffraction patterns (XRDP) of α -Ce₂ON₂, which could be used for the identification of α -Ce₂ON₂ (Figure 3a). Moreover, in Figure 3b, we show the experimental XRPD of the parent AlCo₂Pr₂ type, clearly different from the predicted α -phase of the Ce-O-N compound.

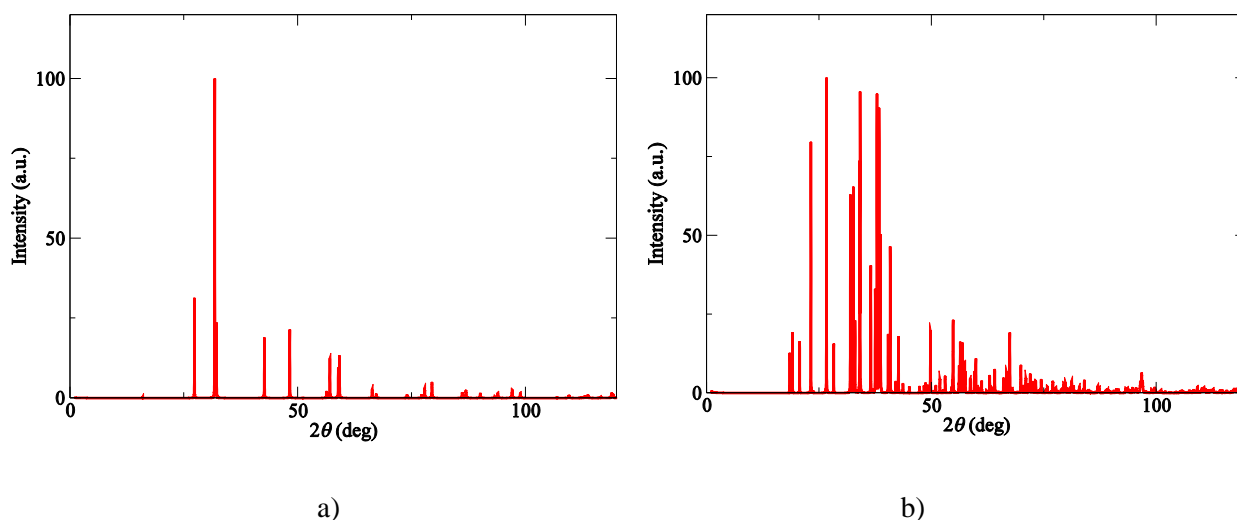


Figure 3. X-ray diffraction patterns (XRDP) of: a) theoretically predicted α -Ce₂ON₂ phase; b) experimentally observed AlCo₂Pr₂ type of structure.

In our investigation, we have calculated elastic constants C_{ij} for the investigated α -Ce₂ON₂ compound up to 10 GPa, in order to get insight into the mechanical stability. Second-order elastic constants for α -Ce₂ON₂ candidates are given in Table 2. It is known from the literature that

eigenvalues of the elastic constant matrix should be all positive in order to have mechanically stable structure. [36] Since this condition is satisfied, the α -Ce₂ON₂ phase should be the mechanically stable phase.

Relation between bulk and shear modulus was calculated to connect the mechanical and elastic properties of the α -Ce₂ON₂ modifications. This simple relation B/K is called Pugh's criterion [37]. According to this criterion, its critical value of 1.75, separates ductile from brittle materials. In the cases when this value is above 1.75, the material exhibits ductile behavior. In contrast, the materials with values of Pugh's criterion under 1.75 have a brittle character. Thus, calculated Pugh's criteria are given in Table 3 and according to them, α -Ce₂ON₂ exhibits ductile behavior. Another insight into ductile/brittle behavior comes from Poisson's ratio ν . For the values of ν smaller than 0.26, the material is expected to have brittle behavior. In this context, we note that according to this criteria α -Ce₂ON₂ has ductile nature. To conclude regardless of the applied criterion (Pugh's or Poisson's), the α -Ce₂ON₂ phase exhibits ductile character, which is important for its future technological applications. This trend continues for the whole investigated pressure range.

Furthermore, hardness V_H is related to the elastic and plastic properties of materials, and can be calculated starting from bulk modulus B and shear modulus K according to equation (1) from Ref. [38]:

$$V_H = 0.92(K/B)^{1.137} K^{0.708} \quad (1)$$

Table 2. The calculated elastic constants of α -Ce₂ON₂ modifications up to 10 GPa.

Pressure (GPa)	C_{11}	C_{12}	C_{13}	C_{33}	C_{44}
0	312.21	180.08	120.02	169.97	103.97
1	318.60	184.60	124.32	174.50	106.08
2	325.18	188.90	129.94	181.98	109.54
3	330.73	192.80	134.63	188.35	111.99
4	337.29	197.02	139.66	189.44	114.70
5	343.31	200.53	143.75	194.50	117.06
6	349.37	204.30	148.63	203.23	119.66
7	355.64	208.20	152.61	209.97	121.99
8	361.73	211.69	156.21	217.16	123.91
9	367.66	215.19	159.88	222.15	125.62
10	373.10	219.05	163.97	230.05	127.55

Table 3. Bulk modulus B (GPa), shear modulus K (GPa), Young's modulus E (GPa), Poisson's ratio (ν), hardness V_H (GPa), and Pugh's criterion, B/K , calculated with LDA in the α -Ce₂ON₂ up to 10 GPa.

Pressure (GPa)	B	K	E	ν	V_H	B/K
0	168.18	72.62	190.46	0.31	7.36	2.32
1	172.85	74.14	194.60	0.31	7.41	2.33
2	178.94	76.28	200.38	0.31	7.51	2.35
3	184.10	77.89	204.80	0.32	7.55	2.36
4	187.85	79.20	208.32	0.32	7.61	2.37
5	192.38	80.91	212.88	0.32	7.71	2.38
6	198.41	82.87	218.23	0.32	7.79	2.39
7	203.49	84.71	223.16	0.32	7.87	2.40
8	208.47	86.52	228.02	0.32	7.96	2.41
9	212.66	88.01	232.02	0.32	8.03	2.42
10	218.02	89.51	236.20	0.32	8.06	2.44

Calculated hardness V_H for the investigated α -Ce₂ON₂ modification in the pressure range 0-10 GPa is given in Table 3. The hardness increases with the applied pressure. In principle, Bulk modulus B , shear modulus K , Young's modulus E , increase more rapidly with the increase of pressure, while Poisson's ratio (ν), hardness (V_H), and Pugh's criterion (B/K), increase more gradually within the same pressure range (Table 3). The mechanical properties of α -Ce₂ON₂ under pressure are very interesting for their scientific and future industrial application.

Electronic properties of the α -Ce₂ON₂ are investigated theoretically. The compound is a semiconductor, with an indirect band gap of ~1.11 eV, with a tendency of the band gap transition from indirect to direct band gap along the H-K special points of the Brillouin zone. Band structure calculation of the α -Ce₂ON₂ has been performed using DFT-LDA functional (Figure 4).

In order to investigate the effect of pressure on the electronic properties of the α -Ce₂ON₂, its behavior up to 10 GPa was investigated. The band gap value at 0 GPa is 1.11 eV and increases linearly with pressure up to 1.17 eV at 10 GPa. Although the band gap widens with the pressure it remains indirect for the whole pressure range. This can be very important for possible band gap tuning of α -Ce₂ON₂ at high pressures, especially since possible change of a direct and indirect band gap indicates applications in e.g. photovoltaics (solar cells) and light-emitting diodes (LEDs).

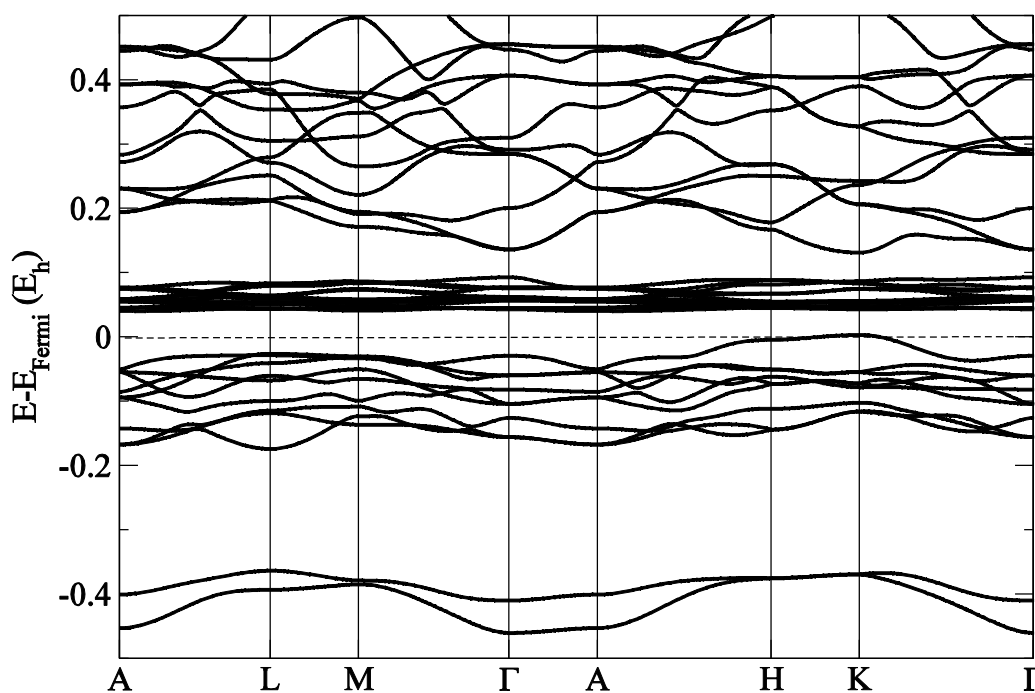


Figure 4. Band structure of the α -Ce₂ON₂ phase. DFT calculations were performed using LDA functional.

4. Conclusion

Detailed investigation of the structure and properties of the α -Ce₂ON₂ have been performed and compared with the related AlCo₂Pr₂ phase. Closely related 8-fold coordination of the α -phase has been presented. Mechanical and elastic properties have been calculated at extreme pressures up to 10 GPa. Investigation of mechanical properties of the α -Ce₂ON₂ indicates the ductile character and mechanical stability of this compound. Bulk modulus, shear modulus, and Young's modulus increase more rapidly with the applied pressure, while Poisson's ratio, hardness, and Pugh's criterion increase more gradually with the increase of pressure (0-10 GPa). Electronic properties are characteristic for semiconductor materials with an indirect band gap of ~1.11 eV and studied under high pressures.

Investigated properties are important for future synthesis and possible application of the investigated α -Ce₂ON₂ compound.

Acknowledgments

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